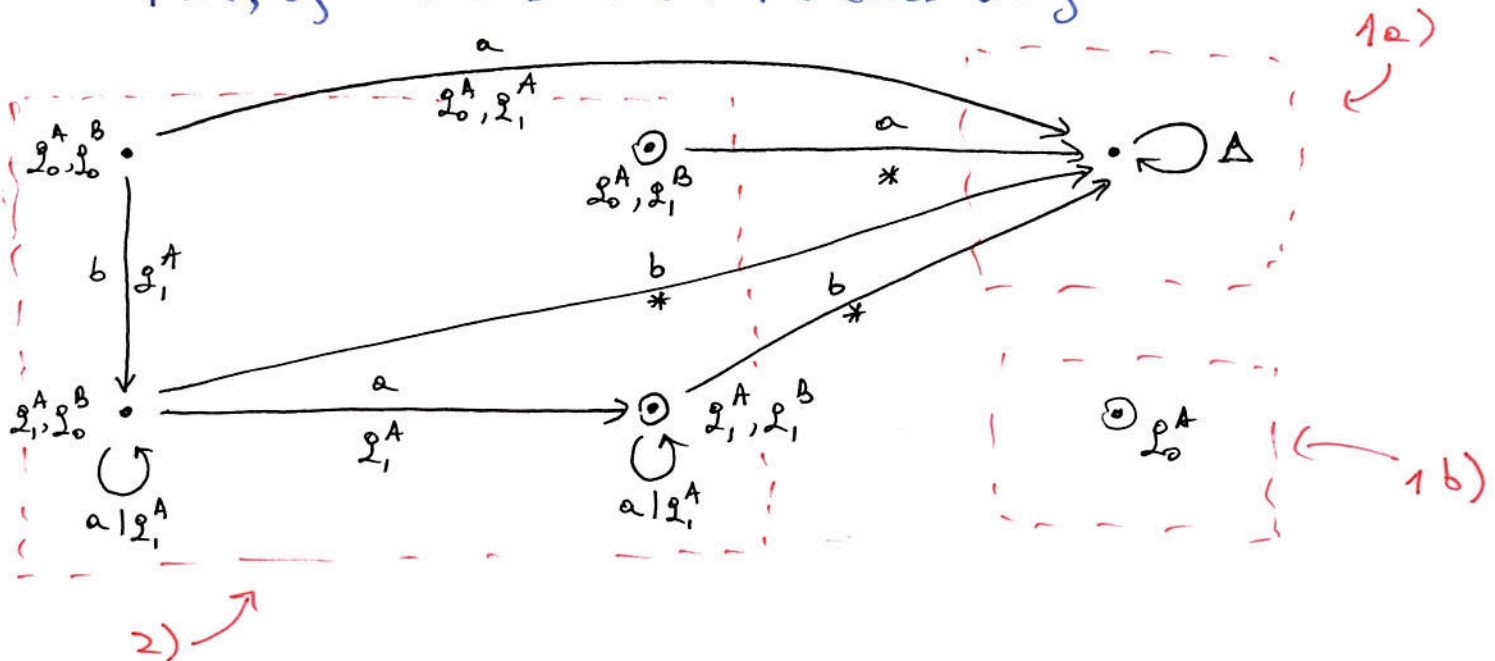


9.1. The NBAs for  $ba^w$  and  $(ab)^* a^w$  are



Then, by the construction in class we get C:



9.2. The only congruence that does not hold out of the given ones is (h).

$$9.3 (a) \neg((\Box p) \rightarrow ((p \wedge \neg r) \cup \neg(oq))) \wedge \neg(\neg p \vee o \diamond r)$$

$$\begin{aligned} & \equiv \Box p \wedge \neg((p \wedge \neg r) \cup \neg(oq)) \quad \wedge \quad \neg(\neg p \vee o \diamond r) \\ & \equiv \Box p \wedge \neg(p \wedge \neg r) \wedge \neg(\neg(oq)) \quad \wedge \quad \neg(\neg p \vee o \diamond r) \\ & \equiv \Box p \wedge (p \wedge r) \wedge (oq) \quad \wedge \quad p \wedge \neg o \diamond r \\ & \equiv \Box p \wedge (p \wedge r) \wedge (oq) \quad \wedge \quad p \wedge \neg o \diamond r \\ & \equiv \Box p \wedge (p \wedge r) \wedge (oq) \quad \wedge \quad p \wedge \neg o \diamond r \\ & \equiv \Box p \wedge (p \wedge r) \wedge (oq) \quad \wedge \quad p \wedge \neg o \diamond r \end{aligned}$$

(b) The proof is a structural induction over LTL which can use PL as base case. The interesting step cases go through because  $\neg(\psi \cup \varphi) \equiv \neg\psi \wedge \neg\varphi$  and  $\neg o\psi \equiv o\neg\psi$ .

3.4.(a) E.g.  $\Box(\varphi \rightarrow \Box\psi) \equiv \Box\neg\varphi \vee (\neg\varphi \wedge \psi)$

(b)  $A \not\models AF \rightarrow \Box\Diamond a$  but  $A \models SF \rightarrow \Box\Diamond a$   
and  $A \models WF \rightarrow \Box\Diamond a$